



# *d*-Wave superconductivity from correlated-hopping interactions determined by angle-resolved photoemission spectroscopy

César G. Galván<sup>a</sup>, Luis A. Pérez<sup>b</sup>, Chumin Wang<sup>a,\*</sup>

<sup>a</sup> Instituto de Investigaciones en Materiales, Universidad Nacional Autónoma de México, A.P. 70-360, 04510, D.F., México, Mexico

<sup>b</sup> Instituto de Física, Universidad Nacional Autónoma de México, A.P. 20-364, 01000, D.F., México, Mexico

## ARTICLE INFO

### Article history:

Received 6 December 2011

Received in revised form 23 February 2012

Accepted 26 February 2012

Available online 3 March 2012

Communicated by R. Wu

### Keywords:

*d*-Wave superconductivity

Hubbard model

ARPES

## ABSTRACT

Starting from a generalized Hubbard model with correlated-hopping interactions, we solve numerically two coupled integral equations within the Bardeen–Cooper–Schrieffer formalism, in order to study the doping effects on the critical temperature ( $T_c$ ), *d*-wave superconducting gap, and the electronic specific heat. Within the mean-field approximation, we determine the single- and correlated-electron-hopping parameters for  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  by using angle-resolved photoemission spectroscopy data. The resulting parametrized Hubbard model is able to explain the experimental  $T_c$  variation with the doping level ( $x$ ). Moreover, the observed power-law behavior of the superconducting specific heat is reproduced by this correlated-hopping Hubbard model without adjustable parameters.

© 2012 Elsevier B.V. All rights reserved.

## 1. Introduction

The microscopic theory developed in 1957 by J. Bardeen, L.N. Cooper and J.R. Schrieffer (BCS) [1] was successful in explaining the main features of metallic superconductors. In the last two decades, the observation of *d*-symmetry pairing in ceramic superconductors has motivated the research of models beyond the standard BCS theory to include anisotropic superconducting gaps. Experimental evidence such as a corner superconducting quantum interference device (SQUID) made of a conventional superconductor and two orthogonally oriented plane faces of a single ceramic superconductor [2], as well as the spontaneous generation of a half-flux quantum at the meeting point of Josephson coupled superconducting crystals [3], strongly suggests a *d*-wave order parameter in many ceramic superconductors. In these materials, the charge carriers are confined to move mainly on the  $\text{CuO}_2$  planes. This quasi-two-dimensional behavior could be essential to understand their superconducting properties. Hence, three-band Hubbard models have been proposed to describe the dynamics of the carriers on the  $\text{CuO}_2$  planes [4], and the electronic states close to the Fermi energy can be reasonably well described by a single-band tight-binding model on a square lattice with a second-neighbor hopping [5]. Furthermore, it has been shown that the second-neighbor correlated-hopping interactions could lead to *d*-wave superconducting ground states [6]. Even in this single-band generalized Hubbard model there are several pa-

rameters that should be determined. In this Letter, we propose a new way to find out single- and correlated-electron-hopping parameters through the angle-resolved photoemission spectroscopy (ARPES) within the mean-field approximation. In particular, we applied this method to  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  systems and found a good agreement between the theoretical results and experimental data of the critical temperature ( $T_c$ ) as well as the electronic specific heat. It is worth mentioning that the tight-binding parameters are usually determined by fitting ARPES data as done in Refs. [7–9], but none of them has further studied  $T_c$  neither specific heat.

## 2. The model

Let us start from a single-band square-lattice Hubbard model with on-site Coulombic interaction ( $U$ ), first- ( $\Delta t$ ) and second-neighbor ( $\Delta t_3$ ) correlated-hopping interactions. Certainly,  $\Delta t$  and  $\Delta t_3$  are always present in real materials and in spite of having small strengths, they are essential in the determination of the superconducting symmetry. The corresponding Hamiltonian can be written as

$$\begin{aligned} \hat{H} = & \varepsilon_0 \sum_{i,\sigma} \hat{c}_{i,\sigma}^+ \hat{c}_{i,\sigma} + t \sum_{\langle i,j \rangle} \hat{c}_{i,\sigma}^+ \hat{c}_{j,\sigma} + t' \sum_{\langle\langle i,j \rangle\rangle} \hat{c}_{i,\sigma}^+ \hat{c}_{j,\sigma} \\ & + U \sum_i \hat{n}_{i,\uparrow} \hat{n}_{i,\downarrow} + \Delta t \sum_{\langle i,j \rangle} \hat{c}_{i,\sigma}^+ \hat{c}_{j,\sigma} (\hat{n}_{i,-\sigma} + \hat{n}_{j,-\sigma}) \\ & + \Delta t_3 \sum_{\substack{\langle\langle i,j \rangle\rangle, \sigma \\ \langle i,l \rangle, \langle j,l \rangle}} \hat{c}_{i,\sigma}^+ \hat{c}_{j,\sigma} \hat{n}_l, \end{aligned} \quad (1)$$

\* Corresponding author.

E-mail address: [chumin@unam.mx](mailto:chumin@unam.mx) (C. Wang).

where  $\hat{c}_{i,\sigma}^\dagger$  ( $\hat{c}_{i,\sigma}$ ) is the creation (annihilation) operator with spin  $\sigma = \downarrow$  or  $\uparrow$  at site  $i$ ,  $\hat{n}_{i,\sigma} = \hat{c}_{i,\sigma}^\dagger \hat{c}_{i,\sigma}$ ,  $\hat{n}_i = \hat{n}_{i,\uparrow} + \hat{n}_{i,\downarrow}$ ,  $\langle i, j \rangle$  and  $\langle\langle i, j \rangle\rangle$  denote respectively first- and second-neighbor sites. This model can lead to  $s$ - and  $d$ -wave superconducting ground states without negative  $U$  [6]. Performing a Fourier transform, this Hamiltonian in the momentum space becomes

$$\begin{aligned} \hat{H} = & \sum_{\mathbf{k},\sigma} \varepsilon(\mathbf{k}) \hat{c}_{\mathbf{k},\sigma}^\dagger \hat{c}_{\mathbf{k},\sigma} \\ & + \frac{1}{N_s} \sum_{\mathbf{k},\mathbf{k}',\mathbf{q}} V_{\mathbf{k},\mathbf{k}',\mathbf{q}} \hat{c}_{\mathbf{k}+\mathbf{q},\uparrow}^\dagger \hat{c}_{-\mathbf{k}'+\mathbf{q},\downarrow}^\dagger \hat{c}_{-\mathbf{k}'+\mathbf{q},\downarrow} \hat{c}_{\mathbf{k}+\mathbf{q},\uparrow} \\ & + \frac{1}{N_s} \sum_{\mathbf{k},\mathbf{k}',\mathbf{q},\sigma} W_{\mathbf{k},\mathbf{k}',\mathbf{q}} \hat{c}_{\mathbf{k}+\mathbf{q},\sigma}^\dagger \hat{c}_{-\mathbf{k}'+\mathbf{q},\sigma}^\dagger \hat{c}_{-\mathbf{k}'+\mathbf{q},\sigma} \hat{c}_{\mathbf{k}+\mathbf{q},\sigma}, \end{aligned} \quad (2)$$

where  $N_s$  is the total number of sites,

$$\varepsilon(\mathbf{k}) = \varepsilon_0 + 2t[\cos(k_x a) + \cos(k_y a)] + 4t' \cos(k_x a) \cos(k_y a), \quad (3)$$

$$\begin{aligned} V_{\mathbf{k},\mathbf{k}',\mathbf{q}} = & U + \Delta t [\beta(\mathbf{q} + \mathbf{k}) + \beta(\mathbf{q} - \mathbf{k}) \\ & + \beta(\mathbf{q} + \mathbf{k}') + \beta(\mathbf{q} - \mathbf{k}')] \\ & + \Delta t_3 [\gamma(\mathbf{q} + \mathbf{k}, \mathbf{q} + \mathbf{k}') + \gamma(\mathbf{q} - \mathbf{k}, \mathbf{q} - \mathbf{k}')], \end{aligned} \quad (4)$$

and

$$W_{\mathbf{k},\mathbf{k}',\mathbf{q}} = \Delta t_3 \gamma(\mathbf{q} + \mathbf{k}, \mathbf{q} + \mathbf{k}'), \quad (5)$$

being

$$\beta(\mathbf{k}) = 2[\cos(k_x a) + \cos(k_y a)], \quad (6)$$

$$\gamma(\mathbf{k}, \mathbf{k}') = 4 \cos(k_x a) \cos(k'_x a) + 4 \cos(k'_y a) \cos(k_y a), \quad (7)$$

and  $2\mathbf{q}$  is the wave vector of the pair center of mass. After a standard Hartree-Fock decoupling of the interaction terms with  $\mathbf{q} \neq \mathbf{0}$  [10] applied to Eq. (2), the reduced Hamiltonian for  $\mathbf{q} = \mathbf{0}$  is

$$\begin{aligned} \hat{H} = & \sum_{\mathbf{k},\sigma} \varepsilon_{MF}(\mathbf{k}) \hat{c}_{\mathbf{k},\sigma}^\dagger \hat{c}_{\mathbf{k},\sigma} + \frac{1}{N_s} \sum_{\mathbf{k},\mathbf{k}'} V_{\mathbf{k},\mathbf{k}',\mathbf{0}} \hat{c}_{\mathbf{k},\uparrow}^\dagger \hat{c}_{-\mathbf{k}',\downarrow}^\dagger \hat{c}_{-\mathbf{k}',\downarrow} \hat{c}_{\mathbf{k},\uparrow} \\ & + \frac{1}{N_s} \sum_{\mathbf{k},\mathbf{k}',\sigma} W_{\mathbf{k},\mathbf{k}',\mathbf{0}} \hat{c}_{\mathbf{k},\sigma}^\dagger \hat{c}_{-\mathbf{k}',\sigma}^\dagger \hat{c}_{-\mathbf{k}',\sigma} \hat{c}_{\mathbf{k},\sigma}, \end{aligned} \quad (8)$$

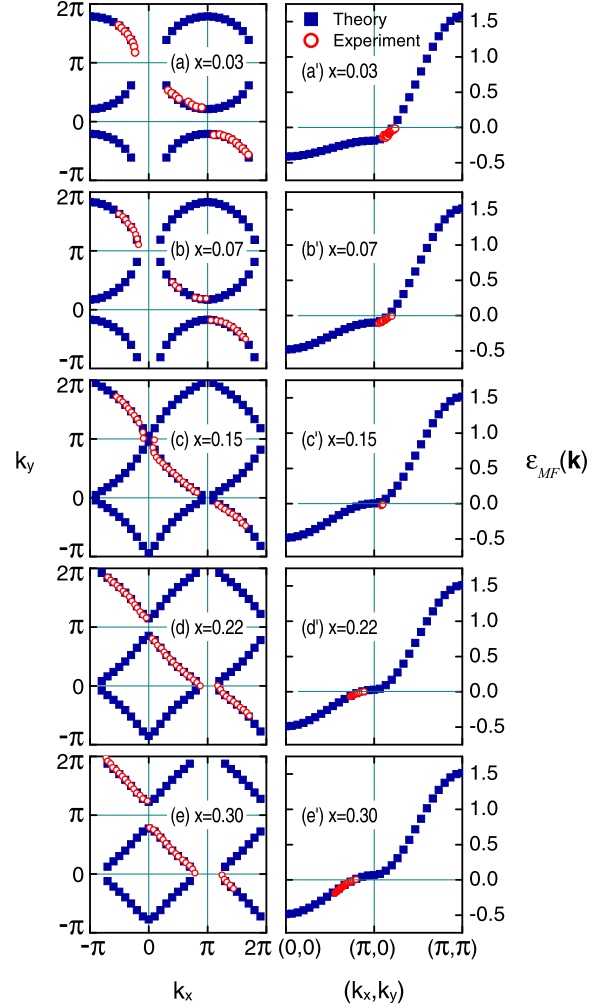
where the mean-field dispersion relation of an effective square lattice with a lattice parameter  $a$  is given by

$$\begin{aligned} \varepsilon_{MF}(\mathbf{k}) = & \varepsilon_{eff} + 2t_{eff}[\cos(k_x a) + \cos(k_y a)] \\ & + 4t'_{eff} \cos(k_x a) \cos(k_y a) \end{aligned} \quad (9)$$

where  $\varepsilon_{eff} = \varepsilon_0 + nU/2$ ,  $t_{eff} = t + n\Delta t$ , and  $t'_{eff} = t' + 2n\Delta t_3$ .

### 3. Parameter determination from ARPES data

Recently, ARPES experiments have been able to determine the electronic dispersion relationship, as well as the anisotropy of superconducting gaps in cuprate superconductors [11]. In particular, such dispersion relationship around the Fermi energy for  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  with different doping levels ( $x$ ) has been measured by extrapolating the peaks of momentum distribution curves up to the Fermi energy ( $E_F$ ) even when the spectral weight is suppressed in going toward  $E_F$  due to the presence of an energy gap or pseudogap [12]. In Figs. 1(a)–(e), the calculated Fermi surfaces (blue solid squares) for  $x = 0.03, 0.07, 0.15, 0.22$  and  $0.30$  are respectively shown and compared with ARPES experimental data (red open circles). Furthermore, Figs. 1(a')–(e') illustrate the corresponding fitted dispersion relations (blue solid squares) along



**Fig. 1.** (Color online.) ARPES data (red open circles) obtained from  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  with different doping levels ( $x$ ) indicated inside in comparison with the calculated dispersion relation (blue solid squares) at the Fermi energy (a)–(e) as well as along the  $(0, 0) - (\pi, 0) - (\pi, \pi)$  direction (a')–(e').

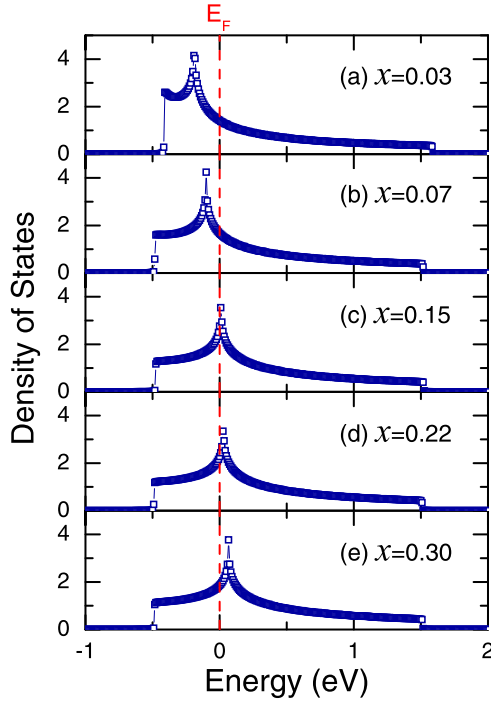
**Table 1**  
Model parameters determined from ARPES data.

$x$	$t_{eff}$ (eV)	$t'_{eff}$ (eV)	$\varepsilon_{eff}$ (eV)	$n$	$\Delta t_3$
0.03	−0.25	0.097	0.199	1.002	0.021
0.07	−0.25	0.077	0.209	0.938	0.021
0.15	−0.25	0.064	0.260	0.761	0.021
0.22	−0.25	0.060	0.268	0.716	0.021
0.30	−0.25	0.056	0.290	0.655	0.021

the  $(0, 0) - (\pi, 0) - (\pi, \pi)$  direction in comparison with experimental ones (red open circles). All the theoretical results of Fig. 1 have been obtained from Eq. (9) and the fitted value of  $\varepsilon_{eff}$ ,  $t_{eff}$ , and  $t'_{eff}$  are summarized in Table 1, where the last two columns  $n$  and  $\Delta t_3$  will be explained below. In particular, we have taken a constant value of  $t_{eff} = -0.25$  eV as in Ref. [12], since only the relative magnitudes of  $t'_{eff}/t_{eff}$  and  $\varepsilon_{eff}/t_{eff}$  are determined by ARPES data.

Once the effective hopping and self-energy parameters are obtained, the electronic density of states (DOS) can be calculated from [13]

$$\text{DOS}(E) = -\frac{1}{\pi} \lim_{\eta \rightarrow 0^+} \text{Im} \left[ \sum_{\mathbf{k}} \frac{1}{E - \varepsilon_{MF}(\mathbf{k}) + i\eta} \right] \quad (10)$$



**Fig. 2.** (Color online.) Electronic density of states (*DOS*) for  $x = 0.03, 0.07, 0.15, 0.22,$  and  $0.30$  corresponding to the mean-field dispersion relation (9) with the effective parameters shown in Table 1.

where  $\varepsilon_{MF}(\mathbf{k})$  is the mean-field dispersion relation given by Eq. (9). The  $DOS(E)$  for  $x = 0.03, 0.07, 0.15, 0.22,$  and  $0.30$  are respectively shown in Figs. 2(a)–(e). Notice that for  $x = 0.15$ , the Fermi level ( $E_F$ ) coincides with the van Hove singularity and then, the critical temperature is expected to be a maximum, according to the BCS theory [1]. By integrating  $DOS(E)$  up to  $E_F$  we obtain the electronic density ( $n$ ), whose numerical values for samples with different doping levels are listed in Table 1, where we observe an increase of the hole concentration from a half-filling electronic band as  $x$  grows.

#### 4. Coupled integral equations

Applying the BCS formalism to Eq. (2), we find the following two coupled integral equations [6,14], which determine the  $d$ -wave superconducting gap  $[\Delta(\mathbf{k})]$  and the chemical potential ( $\mu$ ) for a given temperature ( $T$ ) and electron density ( $n$ ),

$$\Delta(\mathbf{k}) = -\frac{1}{2N_s} \sum_{\mathbf{k}'} \frac{V_{\mathbf{k},\mathbf{k}',\mathbf{0}} \Delta(\mathbf{k}')}{E(\mathbf{k}')} \tanh\left(\frac{E(\mathbf{k}')}{2k_B T}\right) \quad (11)$$

and

$$n - 1 = -\frac{1}{N_s} \sum_{\mathbf{k}'} \frac{\varepsilon_{MF}(\mathbf{k}') - \mu}{E(\mathbf{k}')} \tanh\left(\frac{E(\mathbf{k}')}{2k_B T}\right), \quad (12)$$

where the single-particle excitation energy is given by

$$E(\mathbf{k}) = \sqrt{(\varepsilon_{MF}(\mathbf{k}) - \mu)^2 + \Delta^2(\mathbf{k})}, \quad (13)$$

and  $\Delta(\mathbf{k}) = \Delta_d[\cos(k_x a) - \cos(k_y a)]$ . Eq. (11) can be rewritten as [6]

$$1 = \frac{4\Delta t_3 a^2}{8\pi^2} \int_{-\pi/a}^{\pi/a} \int_{-\pi/a}^{\pi/a} dk_x dk_y \frac{[\cos(k_x a) - \cos(k_y a)]^2}{E(\mathbf{k})} \times \tanh\left(\frac{E(\mathbf{k})}{2k_B T}\right), \quad (14)$$

where the double integral is always positive and then  $\Delta t_3 > 0$  has a key participation in the formation of  $d$ -wave superconducting state within this model, in spite of its relative small strength.

The  $T_c$  can be obtained from Eq. (14) by taking  $\Delta_d(T_c) = 0$  in Eq. (13). For  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ , we chose the maximum  $T_c = 41$  K at  $x = 0.15$  from T. Yoshida et al. [12] to determine the value of  $\Delta t_3$  giving 0.021 eV. In Fig. 3, the calculated  $T_c$  (solid triangles) as a function of the Sr concentration ( $x$ ) is shown and compared with experimental data from N. Momono et al. [15] (open circles) and from T. Yoshida et al. [12] (open squares). Observe that the Fermi energy at the van Hove singularity (see Fig. 2) seems to be a crucial criterion for the determination of maximum  $T_c$ , in accordance with the BCS theory [1,16]. The  $T_c$  as a function of  $n$  calculated by using the Hamiltonian parameters of Table 1 for  $x = 0.15$  (solid squares) and  $x = 0.22$  (solid circles) is illustrated in the inset of Fig. 3, where the corresponding values of  $x$  are indicated by dashed lines.

#### 5. Specific heat results

One of the physical quantities that yields information about the symmetry of superconducting states is the electronic specific heat ( $C_{el}$ ), which is given by [16]

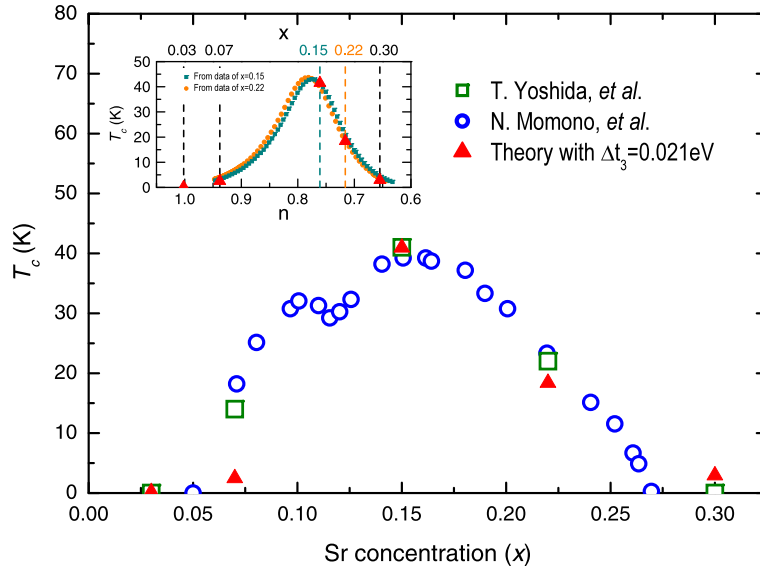
$$C_{el} = \frac{2k_B \beta^2 a^2}{4\pi^2} \int_{\text{BZ}} \int_{\text{BZ}} f[E(\mathbf{k})] \{1 - f[E(\mathbf{k})]\} \times \left[ E^2(\mathbf{k}) + \beta E(\mathbf{k}) \frac{dE(\mathbf{k})}{d\beta} \right] dk_x dk_y, \quad (15)$$

where  $\beta = 1/(k_B T)$  and  $f(E)$  is the Fermi–Dirac distribution. The specific heat of the normal state can be obtained by taking  $\Delta(\mathbf{k})$  equal to zero in Eqs. (13) and (15). In Fig. 4, the calculated  $C_{el}$  (open triangles) for the sample with  $x = 0.15$  using the parameters of Table 1 is shown and compared with the available experimental  $C_{el}$  data obtained from a sample of  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  with a close doping level of  $x = 0.14$  [17]. Notice that the theoretical results reveal an almost second-degree power-law behavior, in agreement with the experimental data, because the low-temperature behavior of  $C_{el}$  is sensitive to the existence of nodes in the gap. However, there is a difference between the theoretical and experimental data about the location and magnitude of the maximum  $C_{el}$ . The former could be due to the sample used for the theoretical calculation has a  $T_c$  of 41 K for  $x = 0.15$ , in contrast to the  $T_c$  of 37 K obtained from the sample of  $x = 0.14$  [17]. The latter might be related to the limitation of our two-dimensional single-band electronic model, instead of a three-dimensional all electron model. In spite of its simplicity, the linear behavior of  $C_{el}$  in the normal state and the discontinuity between the normal and superconducting  $C_{el}$  are well reproduced.

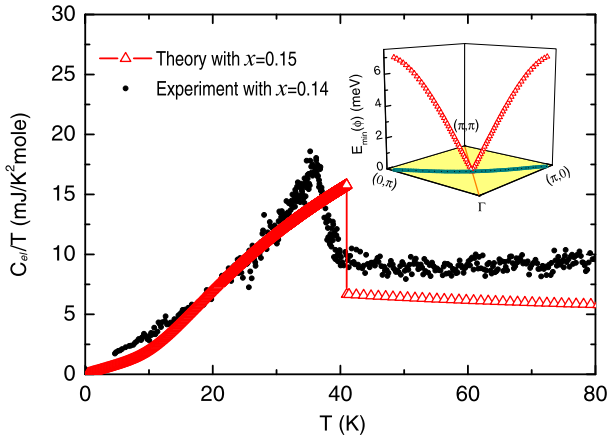
The inset of Fig. 4 presents the first-Brillouin zone scheme of the single excitation energy gap (open triangles) defined as the minimal value of  $E(\phi)$  along  $\phi \equiv \tan^{-1}(k_y/k_x)$  direction. The projection of  $E_{\min}(\phi)$  (green line) on the first-Brillouin zone corresponds to the Fermi surface, shown in Fig. 1(c). Observe that  $E_{\min}(\phi)$  has a  $d$ -wave form with a maximum value of 7.12 meV, which is close to 8.5 meV reported by D.L. Feng et al. [18], 8.6 meV by A. Ino et al. [19], and 13.8 meV by M. Shi et al. [20]. Furthermore, the ratio of the single-excitation energy gap at the antinodal direction, for example at  $\phi = 0$ , over  $k_B T_c$  is 2.015, which is larger than 1.764 from the BCS theory [16].

#### 6. Conclusions

We have presented a generalized Hubbard model, whose parameters were determined by ARPES data for samples of



**Fig. 3.** (Color online.) Theoretical (solid triangles) critical temperature ( $T_c$ ) as a function of the Sr concentration ( $x$ ) in comparison with experimental data of T. Yoshida et al. (open squares) [12] and N. Momono et al. (open circles) [15]. Inset:  $T_c$  versus  $n$  for the Hamiltonian parameters obtained from  $x = 0.15$  (solid squares) and  $x = 0.22$  (solid circles) with the values of  $x$  indicated by dashed lines.



**Fig. 4.** (Color online.) Theoretical (open triangles)  $d$ -wave electronic specific heat ( $C_{el}$ ) versus temperature ( $T$ ) for  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  with  $x = 0.15$  in comparison with the experimental one (solid circles) for  $x = 0.14$  [17]. Inset: Single excitation energy gap (open triangles) in the first-Brillouin zone.

$\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  with different values of  $x$ . The electronic specific heat calculated without adjustable parameters is compared to experimental data and a good agreement is observed. It is worth mentioning that a single-band Hubbard model seems to be enough to reproduce the experimental dispersion relation and the second-neighbor correlated hopping could lead to a  $d$ -wave superconducting ground state with adequate values of  $T_c$ . Furthermore, this model predicts the observed diminution of the electronic density ( $n$ ) from half-filling ( $n = 1$ ) when  $x$  increases. Finally, the van Hove singularity seems to determine  $n$  with maximum  $T_c$ , as found in other models previously studied [21,22].

The present approach can be applied to other compounds including spin triplet superconductors [23]. Also, this study could be extended to include the effects of external perturbations, such as magnetic fields, on the physical properties of anisotropic su-

perconductors, by using the Bogoliubov–de Gennes formalism. This extension is currently being developed [24].

## Acknowledgements

This work has been partially supported by CONACyT-131596, UNAM-IN102511, UNAM-IN107411. Computations have been performed at Bakliz and KanBalam of DGTIC, UNAM.

## References

- [1] J. Bardeen, L.N. Cooper, J.R. Schrieffer, Phys. Rev. 108 (1957) 1175.
- [2] D.A. Wollman, et al., Phys. Rev. Lett. 71 (1993) 2134.
- [3] C.C. Tsuei, J.R. Kirtley, Rev. Mod. Phys. 72 (2000) 969.
- [4] E. Dagotto, Rev. Mod. Phys. 66 (1994) 763.
- [5] H.-B. Schüttler, A.J. Fedro, Phys. Rev. B 45 (1992) 7588.
- [6] L.A. Pérez, C. Wang, Solid State Commun. 121 (2002) 669.
- [7] Z.-H. Pan, et al., Phys. Rev. B 79 (2009) 092507(4).
- [8] H. Ding, et al., J. Phys.: Condens. Matter 23 (2011) 135701(6).
- [9] R.-H. He, et al., Science 331 (2011) 1579.
- [10] E. Dagotto, et al., Phys. Rev. B 49 (1994) 3548.
- [11] A. Damascelli, Z. Hussain, Z.-X. Shen, Rev. Mod. Phys. 75 (2003) 473.
- [12] T. Yoshida, et al., Phys. Rev. B 74 (2006) 224510.
- [13] E.N. Economou, Green's Functions in Quantum Physics, third ed., Springer, Berlin, 2006.
- [14] J.E. Hirsch, F. Marsiglio, Phys. Rev. B 39 (1989) 11515.
- [15] N. Momono, et al., Physica C 233 (1994) 395.
- [16] M. Tinkham, Introduction to Superconductivity, second ed., McGraw-Hill, New York, 1996.
- [17] T. Matsuzaki, N. Momono, M. Oda, M. Ido, J. Phys. Soc. Jpn. 73 (2004) 2232.
- [18] D.L. Feng, et al., Phys. Rev. Lett. 88 (2002) 107001(4).
- [19] A. Ino, et al., Phys. Rev. B 65 (2002) 094504(11).
- [20] M. Shi, et al., Phys. Rev. Lett. 101 (2008) 047002(4).
- [21] J.E. Hirsch, D.J. Scalapino, Phys. Rev. Lett. 56 (1986) 2732.
- [22] R.S. Markiewicz, J. Phys. Chem. Solids 58 (1997) 1179.
- [23] L.A. Pérez, J.S. Millán, C. Wang, Int. J. Mod. Phys. B 24 (2010) 5229.
- [24] C.G. Galván, L.A. Pérez, C. Wang, Bogoliubov–de Gennes analysis of  $d$ -wave superconductors through an ARPES-parameterized Hubbard model, in: The 26th International Conference on Low Temperature Physics, Beijing, China, 2011, Abstract 15P-B004.